

# PILOT Activity Slides

## Differential Equations

Summer 2024



# Welcome to ODE PILOT Session!

## Session Information

- Term: Summer 2024
- Dates: Thursdays between June 6th and July 25th (inc.).
- Time: 8:00pm–10:00pm, Eastern Time.
- Location: Zoom <https://jhubluejays.zoom.us/j/99589950352?pwd=b0JXY3c5ZFpnb2JtchU4LzBIeGx5Zz09>
  - Meeting ID: 995 8995 0352
  - Passcode: 219091
- Leader: James Guo ([sguo45@jhu.edu](mailto:sguo45@jhu.edu))

## PILOT Webpage for ODE

[jhu-ode-pilot.github.io/SU24/](https://jhu-ode-pilot.github.io/SU24/)



# Ground Expectations

In participating the PILOT program, you are expected to:

- Discuss with other students and/or the PILOT leader during meetings, while you may propose any questions and/or concerns if you have any.
- Be respectful and polite to other students during the meetings. If you found any of the contents a mental challenge or uncomfortable, feel free to contact me via email or contact the Director of PILOT at Jenna Hoffman.

## Summer PILOT

Summer PILOT works more like Office Hours, please join the zoom for extra help and review sessions.



# Introducing yourselves

Let's get to know each other.

## Introduction Questions

This section aims to help you introduce yourselves to the other students, please use a few minutes to think about the problems and introduce yourselves to your peers.

Think about yourself. Get ready to introduce yourself by addressing the following information:

- Your name,
- Your expected graduation year,
- Your major(s) and minor(s),
- Your interested area(s) in mathematics.





# ODEs Outreach (Cont.)

- If you can define a mathematical constant, what would you define?
- Do you have a favorite formula/kernel? Name it.
- *Weierstrass Approximate Theorem* guarantees *uniform convergence* for *continuous functions*, whereas *Fourier Convergence Theorem* only guarantees *convergence* for *square integrable functions*. Can you think of some places where you find trade-off situations?
- In mathematics, we call a question *well-posed* if it aligns with the following properties:
  - 1 Existence: There exists at least one solution;
  - 2 Uniqueness: There exists at most one solution;
  - 3 Continuity: The solution depends continuously on the data, *i.e.*, a small error on initial/boundary data entails a small error on the solution.

Can you think of any “well-posed” questions?



# Ordering Game

## Ordered Sets

The field of real numbers is ordered. Thus, each person can select a number, and thus determining an order for the group.

Below are subsets of real numbers, select a number from a set:

- $\left\{0, 1, 2, -1, \frac{1}{2}, \sqrt{2}, \pi, e\right\},$
- $\left\{\sin \frac{2k\pi}{15} : k \in \mathbb{Z} \wedge 0 \leq k \leq 14\right\},$
- $\mathbb{R} \setminus \mathbb{Q}$  (irrational numbers),
- $\left\{\det \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}, \det \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \det \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix}, \det \begin{pmatrix} -1 & 0 \\ -1 & 2 \end{pmatrix}, \right.$   
 $\left. \det \begin{pmatrix} 1 & 3 \\ 4 & 7 \end{pmatrix}, \det \begin{pmatrix} 2 & 0 \\ 0 & 7 \end{pmatrix}, \det \begin{pmatrix} 1 & 0 \\ 4 & 3 \end{pmatrix}, \det \begin{pmatrix} 1 & -2 \\ 12 & 13 \end{pmatrix}\right\},$



# Ordering Game (Cont.)

- $\overline{\mathbb{Q}} \cap \mathbb{R}$  (real, algebraic number),
- $\{f(-10), f(-2), f(0), f(3), f(5), f(20)\}$ ,  
where  $f(x) = \int_0^\infty e^{-xt} \sin t dt$ ,
- $\mathbb{Q}(\sqrt{2}, \sqrt{3}) := \{a + b\sqrt{2} + c\sqrt{3} + d\sqrt{6} : a, b, c, d \in \mathbb{Q}\}$ ,
- $\{n : \text{regular } n\text{-gon is constructible}\}$ ,  
*Hint:* Regular  $n$ -gon is constructible  $\iff \phi(n)$  is an  
integral power of 2,
- $\{F_n\}_n$  (Fibonacci sequence).

## Other Orders?

Of course, there are different ordering methods. For examples, you can look up *dictionary order* for complex numbers.

